



Getting to Mars

Escape velocity

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Launch of the Mars Pathfinder Mission.
NASA/JPL.

The first problem facing a potential trip to Mars is leaving Earth. Specifically, this problem deals with the enormous amount of energy necessary to break free from the Earth's gravitational field and start traveling towards Mars, or anywhere else in the Solar System. To find out what energy, and therefore speed, is necessary to escape Earth's gravity, let us consider the energy of a rocket at Earth's surface:

$$E = \frac{1}{2} m_{\text{rocket}} v_{\text{initial}}^2 - GM_{\text{earth}} m_{\text{rocket}} / R_{\text{earth}}$$

Energy is the sum of kinetic and potential energies. Here, v_{initial} is the initial velocity, m_{rocket} is the mass of the rocket, and M_{earth} and R_{earth} are the mass of the Earth and the radius of the

Earth. Now, because the energy of the rocket is constant as it travels upward, we can equate the energy of the rocket at the surface to the energy of the rocket at its maximum altitude:

$$\frac{1}{2} m_{\text{rocket}} v_{\text{initial}}^2 - GM_{\text{earth}} m_{\text{rocket}} / R_{\text{earth}} = \frac{1}{2} m v_{\text{final}}^2 - GM_{\text{earth}} m_{\text{rocket}} / r_{\text{maximum}}$$

Here, v_{final} is the final velocity and r_{maximum} is the maximum height. However, at its maximum height, $v_{\text{final}} = 0$, so the equation becomes

$$\frac{1}{2} m_{\text{rocket}} v_{\text{initial}}^2 - GM_{\text{earth}} m_{\text{rocket}} / R_{\text{earth}} = -GM_{\text{earth}} m_{\text{rocket}} / r_{\text{maximum}}$$

Solving for v_i , we have

$$v_{\text{initial}}^2 = 2GM_{\text{earth}}(1/R_{\text{earth}} - 1/r_{\text{maximum}})$$

Setting $r_{\text{maximum}} = \infty$, which is the condition for gravitational escape, v_{initial} becomes v_{escape} and we have

$$v_{\text{escape}} = \text{sqrt}(2GM_{\text{earth}}/R_{\text{earth}})$$

The same logic can be applied to any planet, so the equation for escape velocity can be generalized to

$$v_{\text{escape}} = \text{sqrt}(2GM/R)$$

Thus, the escape velocity from any planet depends on the mass of the planet and the radius of the planet. For example, let us assume that we have a spacecraft on Earth that we are trying to send into space. $M_{\text{earth}} = 5.98 \times 10^{24}$ kg, and $R_{\text{earth}} = 6.37 \times 10^6$ m, so we get:

$$v_{\text{escape}} = \text{sqrt}(2GM/R)$$

$$v_{\text{escape}} = \text{sqrt}\left(\frac{2(6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2)(5.98 \times 10^{24} \text{ kg})}{(6.37 \times 10^6 \text{ m})}\right)$$

$$v_{\text{escape}} = 1.12 \times 10^4 \text{ m/s, or about 11 km/s.}$$

Now, let us assume astronauts have successfully completed their mission on Mars and need to calculate the escape velocity on Mars so they can travel back to Earth. $M_{\text{mars}} = 6.42 \times 10^{23}$ kg, and $R_{\text{mars}} = 3.397 \times 10^6$ m, so we get:

$$v_{\text{escape}} = \text{sqrt}(2GM/R)$$

$$v_{\text{escape}} = \text{sqrt}\left(\frac{2(6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2)(6.42 \times 10^{23} \text{ kg})}{(3.397 \times 10^6 \text{ m})}\right)$$

$$v_{\text{escape}} = 5.0 \times 10^3 \text{ m/s, or about 5 km/s.}$$

The Benchmark Lessons were developed with the help of the following sources:

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